# Chessboard Condition 

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The only reason I'm writing this is because I saw other people do some really complicated stuff with their if statements, or using some weird long method. It's actually really simple, so I thought I'd write this to explain my method.

Here's my very simple if statement.

$$
\text { if }((i / 64+j / 64) \% 2==0)
$$

This takes advantage of the fact that i/64 acts as the floor function, so we have mapped every point of the form

$$
(x, y), \quad 0 \leq x, y<512
$$

into a point

$$
(x, y), \quad 0 \leq x, y<8
$$

Note that we can compute a sum table as below:

|  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| 1 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 3 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| 4 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 |
| 5 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| 6 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 |
| 7 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |

We can take these sums mod 2.

|  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | 1 | 0 | 1 | 0 | 1 | 0 | 1 |
| 1 | 1 | 0 | 1 | 0 | 1 | 0 | 1 | 0 |
| 2 | 0 | 1 | 0 | 1 | 0 | 1 | 0 | 1 |
| 3 | 1 | 0 | 1 | 0 | 1 | 0 | 1 | 0 |
| 4 | 0 | 1 | 0 | 1 | 0 | 1 | 0 | 1 |
| 5 | 1 | 0 | 1 | 0 | 1 | 0 | 1 | 0 |
| 6 | 0 | 1 | 0 | 1 | 0 | 1 | 0 | 1 |
| 7 | 1 | 0 | 1 | 0 | 1 | 0 | 1 | 0 |

And the chessboard pattern is now clear within this table. We just take $x+y$ and check whether it is 0 or 1 $\bmod 2$.

The full function is on the next page.

```
void drawChessboard(pixel pixels[BOARD_SIZE][BOARD_SIZE]) {
    for (int i = 0; i < BOARD_SIZE; i++) {
            for (int j = 0; j < BOARD_SIZE; j++) {
                if ((i/64 + j/64) % 2 == 0) { // this is the line which is different
                // black
                pixels[i][j].red = 0;
                pixels[i][j].green = 0;
                pixels[i][j].blue = 0;
            } else {
                // white
                pixels[i][j].red = 255;
                pixels[i][j].green = 255;
                pixels[i][j].blue = 255;
            }
        }
    }
}
```

